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Quantitative evaluation of defect-models in superconducting phase qubits

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We use high-precision spectroscopy and detailed theoretical modeling to determine the form of the coupling between a superconducting phase qubit and a two-level defect. Fitting the experimental data with our theoretical model allows us to determine all relevant system parameters. We observe a strong qubit-defect coupling with a nearly vanishing longitudinal component. We quantitatively compare several existing theoretical models for the microscopic origin of two-level defects. © 2010 American Institute of Physics. [doi:10.1063/1.3529457]

A key limiting factor of superconducting quantum coherent devices is that they suffer from decoherence induced by their weak but non-negligible interaction with the environment,1 the details of which are still not completely understood. One such enigma is the appearance of pronounced anticrossings in the spectra of superconducting phase4 and flux3 qubits, which are indicative of a strong interaction with an additional quantum system. It has been shown that these are coherent two-level, or at least strongly anharmonic,5 defects, but their exact microscopic nature is still unclear.

In several experiments,3–5 it has been observed that, for strongly coupled defects, the coupling term is transverse (involving pure qubit-defect energy exchange) with minimal longitudinal (phase shift inducing) component. In this work, we perform a high-precision comparison between experimental data and a general theoretical model to shed light on the exact form of the coupling operator between qubit and two-level defect. We obtain quantitative estimates of the longitudinal and transverse components and then compare our results to existing theoretical models for intrinsic two-level systems.

We theoretically describe the system of qubit and two-level system (TLS) by the Hamiltonian

\[ H = H_q + H_{TLS} + H_I, \]

where \( H_q \) describes the qubit, \( H_{TLS} \) describes the TLS, and \( H_I \) describes the interaction between the two. Our qubit is a flux biased phase qubit,6,7 consisting of a superconducting ring interrupted by a Josephson junction and threaded by an external flux. The qubit Hamiltonian is given by

\[ H_q = \frac{2e^2}{C} q^2 - E_j \cos \phi + \frac{1}{2L} \left( \Phi_0 / 2\pi \right)^2 (\phi - \phi_{ext})^2, \]

where \( E_j = I_c \Phi_0 / 2\pi \) is the Josephson energy of the circuit, \( C \) is the qubit’s capacitance, \( L \) is the inductance of the superconducting ring, and \( \Phi_0 \) is the superconducting flux quantum. Equation (2) describes an anharmonic oscillator with dynamical variables given by the phase difference across the Josephson junction \( \phi \) and its conjugate momentum \( \dot{q} \), corresponding to the number of Cooper-pairs tunneled across the junction, with \( [\dot{q}, \phi] = i \). The external flux \( \phi_{ext} \) is generated via a flux coil on chip. We assume a linear flux-current relation of the form \( \phi_{ext} = \alpha \text{bias} + \beta \), with the fabrication dependent parameters \( \alpha \) and \( \beta \). The TLS is described as a generic two-level system, and we write its Hamiltonian in the eigenbasis \( H_{TLS} = \frac{1}{2} \epsilon_{TLS} \tau_z \), with the level splitting \( \epsilon_{TLS} \) and the Pauli-matrix \( \tau_z \).

We consider three different coupling operators, which may stem from fluctuations in the three terms of Eq. (2), each of which corresponds to a different microscopic origin. The state of the TLS may modulate the magnetic flux \( \phi_{ext} \) threading the superconducting loop6,7 or the critical current \( I_c \) of the Josephson junction,8–11 resulting in coupling to \( \phi \) or \( \cos \phi \), respectively. Alternatively, the TLS may couple to the electric field of the junction \( E \propto \dot{q} \), which is consistent with the TLS being formed from a charge-dipole.12,13 These three situations are described by the following coupling Hamiltonians \( H_I \):

\[ H_I^{(\delta)} = v_{\delta}(\cos \theta \tau_x \pm \sin \theta \tau_z), \]

where \( \delta = \dot{q}, \phi, \) or \( \cos \phi \) depending on the nature of the coupling and \( v_\delta \) parameterizes its strength. The angle \( \theta \in [0, \pi] \) denotes the relative orientation of the TLS eigenbasis, the physical meaning of which depends on the particular microscopic model.

In order to compare the various coupling models, we define the transverse \( v_\perp \) and longitudinal \( v_\parallel \) couplings in the qubit \((|0\rangle, |1\rangle)\) basis as

\[ 2v_\perp = v_{\delta} \cos \theta \delta (|1\rangle \langle 0| + |0\rangle \langle 1|), \]

\[ 2v_\parallel = v_{\delta} \sin \theta \delta (|1\rangle \langle 1| - |0\rangle \langle 0|), \]

where the qubit component of the coupling term \( \delta \) is defined as in Eq. (3).

To shed light on the nature of the interaction between qubit and two-level defect, we need to determine the values of \( v \) and \( \theta \). To this end, we have performed a series of spectroscopy experiments of a superconducting phase qubit.
strongly coupled to a TLS, at varying microwave power; see Fig. 1. Performing spectroscopy at both low- and high-power allows us to use a combination of single- and two-photon transitions to obtain spectral lines that are sensitive to the nature of the qubit-TLS coupling. We also performed “swap-spectroscopy,” where an additional swap between qubit and TLS is performed before readout, effectively measuring the state of the TLS. We extract the frequencies of the various transitions in the coupled system by fitting each spectroscopic trace with Lorentzian functions.

Our theoretical model, Eq. (1), can be described by a total of six independent parameters. Three parameters describe the qubit circuit and its tuning via the external flux: the critical current $I_c$ of the qubits Josephson junction and the parameters $\alpha$ and $\beta$ describing the local generation of flux on chip and its coupling to the qubit loop. The TLS is described by its level splitting $\epsilon_{\text{TLS}}$ and the interaction between qubit and TLS via $\nu$ and $\theta$. Figure 2 shows an illustration of the spectrum of the model and the influences of the different parameters. Since their effects on the spectrum, as indicated by arrows in Fig. 2, are all largely independent, this allows us to perform a fit to all six parameters simultaneously. For the circuit capacitance $C$ and inductance $L$ we take the design values of $C=850$ F and $L=720$ pH. To account for fabrication variation, we repeated the fitting procedure with a ±5% tolerance in both $L$ and $C$, resulting in no significant variation in the TLS parameter estimates (although $I_c$, $\alpha$, and $\beta$ vary accordingly). It is important to note that, since we are limited to spectroscopic data, our results are only sensitive to purely transversal $\pm \sigma_z \tau_z$ and purely longitudinal $\pm \sigma_x \tau_x$ coupling terms.

As an example, the estimated parameters for coupling to critical current according to Eq. (3) are level splitting $\epsilon_{\text{TLS}}=7944.38 \pm 0.08$ MHz with coupling strengths $\nu_\perp = 35.52 \pm 0.13$ MHz and $\nu_\parallel = 0.27 \pm 0.12$ MHz (uncertainties correspond to 1–σ confidence intervals throughout). We find that the estimates obtained by fitting to each of the three coupling models are consistent with each other. Repeating the fitting for an additional defect in the same chip with different level splittings $\epsilon_{\text{TLS}}$ and coupling parameters $\nu$ and $\theta$ produced qualitatively similar results, so we only consider one TLS in what follows. Full details can be found in the supplementary material.

We now discuss our results in light of several existing models describing the microscopic origin of such TLSs.

\[ \phi_{\text{Ext}} = \alpha I_{\text{bias}} + \beta \]
Coupling to either magnetic flux or critical current generates both transverse and longitudinal components. Using the ratio of these terms gives us an estimate for the orientation of \( \tan \theta = 0.04 \pm 0.02 \) for either coupling, placing strong constraints on critical current or magnetic flux coupling models.

If the state of the TLS modulates the value of the magnetic flux threading the superconducting loop, the observed coupling would result from a spin in the surface of the superconducting loop. Although the data are compatible with a small longitudinal coupling component, it is possible that a small longitudinal coupling could result from a magnetic flux contribution of \( \phi_0 \). Using our estimates for the transverse component gives us an estimate for the orientation of \( \tan \theta = 0.08 \). Since the momentum operator has no diagonal component, this type of interaction would not lead to a longitudinal component \( \sigma_z \tau_z \) in the coupling operator.

Using general theoretical models and high resolution spectroscopy, we have estimated the various coupling parameters between a superconducting phase qubit and a coherent two-level system within the qubit circuit. Comparing with existing theoretical models, we obtained parameter estimates for various suggested sources of such defects. In each case, the experimental data indicate a small or nonexistent longitudinal coupling, relative to the transverse coupling term. These results allow us to place strong constraints on the parameters of the theoretical models and test their validity.

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14. See supplementary material at http://dx.doi.org/10.1063/1.3529457 for further details of the calculations and parameter estimates.